

## Durham Research Online

---

### Deposited in DRO:

02 December 2014

### Version of attached file:

Accepted Version

### Peer-review status of attached file:

Peer-reviewed

### Citation for published item:

Milledge, D.G. and Griffiths, D. and Lane, S.N. and Warburton, J. (2012) 'Limits on the validity of infinite length assumptions for modelling shallow landslides.', *Earth surface processes and landforms.*, 37 (11). pp. 1158-1166.

### Further information on publisher's website:

<http://dx.doi.org/10.1002/esp.3235>

### Publisher's copyright statement:

This is the accepted version of the following article: Milledge, D. G., Griffiths, D. V., Lane, S. N. and Warburton, J. (2012), Limits on the validity of infinite length assumptions for modelling shallow landslides. *Earth Surface Processes and Landforms*, 37 (11): 1158–1166, which has been published in final form at <http://dx.doi.org/10.1002/esp.3235>. This article may be used for non-commercial purposes in accordance With Wiley Terms and Conditions for self-archiving.

### Additional information:

## Use policy

---

The full-text may be used and/or reproduced, and given to third parties in any format or medium, without prior permission or charge, for personal research or study, educational, or not-for-profit purposes provided that:

- a full bibliographic reference is made to the original source
- a [link](#) is made to the metadata record in DRO
- the full-text is not changed in any way

The full-text must not be sold in any format or medium without the formal permission of the copyright holders.

Please consult the [full DRO policy](#) for further details.

**Limits on the validity of infinite length assumptions for  
modelling shallow landslides**

Journal:	<i>Earth Surface Processes and Landforms</i>
Manuscript ID:	ESP-11-0234.R1
Wiley - Manuscript type:	Paper
Date Submitted by the Author:	14-Dec-2011
Complete List of Authors:	Milledge, David; Durham University, Institute of Hazard Risk and Resilience; Durham University, Department of Geography Griffiths, D; Colorado School of Mines, Division of Engineering Lane, Stuart; Université de Lausanne, Institut de géographie Warburton, Jeff; Durham University, Department of Geography
Keywords:	infinite slope length, stability model, shallow landslide, finite element method, benchmark

SCHOLARONE™  
Manuscripts

**Limits on the validity of infinite length assumptions for modelling shallow landslides**

**Abstract**

The infinite slope method is widely used as the geotechnical component of geomorphic and landscape evolution models. Its assumption that shallow landslides are infinitely long is usually considered valid for natural landslides on the basis that they are generally long relative to their depth. However, this is rarely justified because we lack a clear definition of the critical length / depth ratio below which edge effects become important and length dependence appears. Here we benchmark infinite slope predictions across the range of possible slope properties found on natural slopes to establish the critical length at which infinite slope stability predictions fall within 5 and 10% of those estimated by a finite element method. We find that infinite slope stability predictions always converge to within 5% of the finite element benchmarks at a critical length / depth ratio of 25. However, they can converge at much lower ratios depending on slope properties, particularly the proportions of cohesive versus frictional soil strength so that critical length depth ratios are smaller for low cohesion soils. As a result the infinite length assumption within the infinite slope method is valid for catchment scale models when their grid resolution is coarse (e.g. >25 m). However, it may also be important when their grid resolution is much finer, because spatial organisation in the predicted pore water pressure field reduces the probability of short landslides and minimises the risk that predicted landslides will have length / depth ratio's less than 25.

Keywords: infinite slope length, stability model, shallow landslide, finite element method, benchmark.

## Background

Shallow landslides are important agents of erosion and sources of sediment in terrestrial environments and need to be represented in geomorphic (e.g. Montgomery and Dietrich, 1994; Bathurst *et al.*, 2005; Reid *et al.*, 2007) and landscape evolution models (e.g. Tucker and Bras, 1998). However, a full stability analysis at every potential landslide site is not feasible; therefore much work has focussed on trying to develop simple physically based methods to identify shallow landslide risk comparatively across the landscape (e.g. Montgomery and Dietrich, 1994; Baum *et al.*, 2008).

The infinite slope method (Taylor, 1948; Haefeli, 1948; Skempton and DeLory, 1957) is widely used as the geotechnical component of these geomorphic and landscape evolution models where it is generally combined with a hydrological model to predict pore water pressure and hence failure probability. Much attention in developing these models has been focussed on different approaches to predicting the spatial pore water pressure patterns (Montgomery and Dietrich, 1994; Burton and Bathurst, 1995; Wu and Sidle, 1995; Reid *et al.*, 2007; Simoni *et al.*, 2008; Baum *et al.*, 2008). However, much less attention has been given to the geotechnical component. This is partly because the assumptions behind the infinite slope method, particularly of infinite width and length (Skempton and DeLory, 1957), are considered valid for many natural landslides, which have relatively high length ( $L$ ) / depth ( $H$ ) ratios (Haneberg, 2004). Furthermore, attempts to account for the influence of the landslide margins on the balance of forces requires additional assumptions to be made about the location, orientation, and magnitude of the forces involved.

The argument that the infinite slope method is suitable for shallow landslides because they have high length / depth ( $L/H$ ) ratios is frequently stated but rarely justified (Wu and Sidle, 1995; Iverson, 2000; Crosta and Frattini, 2002; Casadei *et al.*, 2003; Haneberg, 2004; Bathurst *et al.*, 2005; Ray *et al.*, 2010). Most natural landslides are shallow, Figure 1 shows two example inventories where  $L/H$  ratios exceed 7 for >90% of landslides (Gabet and Dunne, 2002; Warburton *et al.*, 2008), while the

1 51 scaling analysis of Larsen *et al.* (2010) suggests  $L/H$  ratio increases with length ( $L/H = 12.5 L^{0.16}$ )  
2 52 and exceeds 18 even for very small landslides ( $L < 4$  m). However, we cannot assume that the infinite  
3 53 slope method is suitable for these landslides without more rigorous testing. This requires an  
4 54 assessment of the  $L/H$  ratio of the predicted or observed landslides relative to the  $L/H$  ratio at which  
5 55 infinite slope assumptions break down.  
6 56  
7 57 <Figure 1 near here>  
8  
9 58  
10  
11  
12  
13  
14  
15  
16  
17  
18 59 Recent work by Griffiths *et al.* (2011) has begun to address this by benchmarking infinite slope  
19  
20 60 predictions against those from a finite element (FE) continuum mechanics method. The rationale for  
21  
22 61 this is that the FE predictions can be assumed as a benchmark for the stability of a given slope. This  
23  
24 62 is reasonable since they have been shown to be reliable and robust for assessing the factor of safety  
25  
26 63 of slopes across a range of scenarios (Griffiths and Lane, 1999). They perform at least as well as  
27  
28 64 limit equilibrium methods for known parametric tests (Hammah *et al.*, 2005) but are far more  
29  
30 65 flexible, not requiring assumptions about: the shape or location of the failure surface, nor the inter-  
31  
32 66 slice forces (Griffiths and Lane, 1999). On this basis, infinite slope stability predictions can then be  
33  
34 67 tested against the FE predictions for different slope lengths.  
35  
36  
37  
38 68  
39  
40 69 Griffiths *et al.* (2011) find that the FE predictions converge on those from the infinite slope method  
41  
42 70 at  $L/H$  ratios of around 16 and suggest that, in general, the infinite slope method is suitable for  $L/H >$   
43  
44 71 16. However they show that for slopes with shorter  $L/H$  ratios the infinite slope method predictions  
45  
46 72 become increasingly different to the benchmark as  $L/H$  decreases. At an  $L/H$  ratio of two, the infinite  
47  
48 73 slope method can predict that a slope is less than half as stable as the FE method predicts for the  
49  
50 74 same slope. They attribute this difference to error in the infinite slope method resulting from the  
51  
52 75 violation of its infinite length assumption. This has potentially significant implications for the  
53  
54 76 appropriateness of the infinite slope method for geomorphic modelling. Such models often rely on  
55  
56 77 cell-by-cell calculations of infinite-slope stability with resolutions ranging from a few to tens of  
57  
58 78 meters. The often implicit assumption in applying these models is that the grid cells are adequately  
59  
60

long relative to the landslide failure plane depth so that factors of safety calculated with an infinite slope approach are reasonably free of error. If the findings of Griffiths *et al.* (2011) hold across the full range of natural slope conditions then this assumption would be valid for models with grid cells longer than 16 times the assumed failure plane depth but could introduce error at finer resolutions. In this paper we extend some of the initial conclusions from Griffiths *et al.* (2011) to establish the generality of their findings; then assess the implications of these findings for stability analysis within geomorphology and landscape evolution models.

### ***The Infinite Slope Method***

The most common geotechnical measure of slope stability is the factor of safety (*FoS*) the ratio of shear strength of the soil (*s*) to the shear stress (*τ*) required for equilibrium.

**Equation 1**

$$FoS = \frac{s}{\tau}$$

A slope is considered to be just stable when the stresses and strengths are equal and the *FoS* is equal to one and to fail for *FoS* < 1. The factor of safety can be calculated using a range of approaches, including the one dimensional infinite slope method, and more sophisticated limit equilibrium and continuum mechanics methods in two and three-dimensions. More sophisticated methods allow improved representation of the failure geometry. However, they require fine scale discretisation of the slope, phreatic surface and failure plane geometries and generally need to be solved iteratively. These data and computational requirements limit their applicability at the catchment scale where analysis almost invariably involves the simpler one-dimensional infinite slope method.

<Figure 2 near here>

The Infinite Slope (IS) method (Taylor, 1948; Haefeli, 1948; Skempton and DeLory, 1957) makes two key assumptions: 1) that sliding occurs along a pre-defined plane parallel to the face of the slope; and 2) that the sliding block is infinitely long and wide so that stresses are the same on the two

planes perpendicular to the slope (e.g. stresses A-A' = stresses B-B' in Figure 2). These stresses are collinear, equal in magnitude and opposite in direction. Therefore they exactly balance each other and can be ignored. The equilibrium equations are derived using a rectangular block (e.g. A-B-B'-A'). All the stresses perpendicular ( $\sigma$ ) and parallel ( $\tau$ ) to the failure plane are summed to give:

$$\tau = W \sin \beta = \gamma_s H \cos \beta \sin \beta \quad \text{Equation 2}$$

$$\sigma = \cos \beta W = \cos^2 \beta \gamma_s H \quad \text{Equation 3}$$

where:  $\beta$  is the block's slope [-];  $W$  is the weight of the block [kN];  $\sigma$  is the normal stress on the slip plane [kPa];  $\gamma_s$  is the soil unit weight [ $\text{kN m}^{-3}$ ]; and  $H$  is the vertical depth to the shear plane [m]. Assuming steady seepage parallel to the slope at a depth of  $H_w$  above the failure plane [m], we can account for the effect of pore water pressure ( $u$ ) [kPa] on normal stress to calculate the effective normal stress using:

$$\sigma - u = \cos^2 \beta (\gamma_s (H - H_w) + (\gamma_s - \gamma_w) H_w) = \cos^2 \beta H (\gamma_s - \gamma_w m) \quad \text{Equation 4}$$

where:  $\gamma_w$  is the water unit weight [ $\text{kN m}^{-3}$ ]; and  $m$  is the normalised free surface height [-] defined as  $m = H_w/H$ ;  $m=1$  for fully saturated flow with the phreatic surface at the ground surface, and  $m=0$  for "dry" cases where the phreatic surface is below the failure plane and does not affect the stability.

Shear strength ( $s$ ) [kPa] for effective stresses is expressed by the Mohr–Coulomb equation as:

$$s = c' + (\sigma - u) \tan \varphi' \quad \text{Equation 5}$$

where:  $c'$  is the effective soil cohesion [kPa]; and  $\varphi'$  is the effective friction angle [-]. Substituting Equation 2, Equation 3 and Equation 5 into Equation 1 to calculate the factor of safety ( $FoS$ ) [-] gives:

$$FoS = \frac{c' + \cos^2 \beta H (\gamma_s - \gamma_w m) \tan \varphi'}{\gamma_s H \cos \beta \sin \beta} \quad \text{Equation 6}$$

This provides a very simple one-dimensional balance of forces equation for slope stability that can be easily applied within a spatial model for landslides since the stability of each element can be calculated independent of its neighbours.

135

1  
2 136 However, its validity and predictive ability is defined by the extent to which its assumptions are met.  
3  
4 137 Griffiths *et al.*, (2011) have suggested that the infinite length assumption is reasonable for  $L/H$  ratios  
5  
6 138 greater than 16. However, before we can use this as a critical  $L/H$  ratio when assessing the suitability  
7  
8 139 of the infinite slope method for catchment modelling we need to know: 1) how general this result is  
9  
10 140 under the range of plausible conditions found in natural landscapes; and 2) which slope properties, if  
11  
12 141 any, influence the magnitude of the critical  $L/H$  ratio.  
13  
14  
15  
16  
17

142

## 143 Method

### 144 *Parameter exploration*

145 To address these questions we explored the influence of  $L/H$  ratio on the accuracy of the infinite  
146 slope method by benchmarking it against the same finite element method as Griffiths *et al.* (2011).  
147 To establish the generality of the relationships we varied all the other parameters within the infinite  
148 slope equation (Equation 6, cohesion, friction angle, soil depth, normalised free surface height, soil  
149 unit weight and slope angle). We varied these parameters across their reasonable ranges (Table 1)  
150 and assessed the impact of these variations on the critical  $L/H$  ratio ( $L/H_{crit}$ ) at which the infinite  
151 slope predictions converged with those from the finite element method.

152

153 Our experimental design for the parameter exploration had two components. First, we used a  
154 systematic parameter exploration to test the method's performance for a set of extreme parameter  
155 combinations at the limits of the parameter space. The parameters and their limits are listed in Table  
156 1. In each case we used the FE method to predict  $FoS$  at  $L/H$  ratios of: 4, 8, 12, 16, 24 and 48. These  
157 ratios were chosen after initial tests in order to sample most densely in the region of expected  
158 convergence for the two methods but with some samples at longer  $L/H$  ratios to ensure that any  
159 extreme responses were captured. We then compared the FE and IS predictions, standardising the  
160 results by expressing the difference between predictions as a percentage of the FE  $FoS$ . The  
161 systematic parameter exploration is useful in illustrating the form of the  $FoS$  difference curves across



162 the reasonable range of slope properties. However, it is difficult to interpret in terms of the influence  
163 of individual parameters on the  $L/H_{crit}$  value because: 1) it only shows results for the extreme limits  
164 to the slope properties; and 2) the parameter combinations are difficult to differentiate.  
165  
166 Second, we addressed the limitations above using a random parameter exploration. Here, we applied  
167 a Monte Carlo approach, sampling each of the six infinite slope parameters randomly and assuming a  
168 uniform distribution across the range defined in Table 1. Although some of the parameters in the IS  
169 method tend to co-vary (e.g.  $\phi'$  and  $c'$ ) we sampled from uniform distributions and avoided *a priori*  
170 assumptions about their covariance because we were interested in the sensitivity of the method to the  
171 full range of possible conditions and so needed broad and uniform coverage of the parameter space.  
172 This generated 5000 synthetic slopes with random slope geometry and material properties. For each  
173 of these we then calculated stability using the FE and IS methods for the same set of  $L/H$  ratios used  
174 in the first parameter exploration. Again the error in the IS predictions was expressed as a percentage  
175 of the FE  $FoS$ . The  $L/H_{crit}$  at which the FE method converged to within 5% and 10% of the IS  
176 predictions was recorded. These critical  $L/H$  ratios could then be plotted against each parameter to  
177 show the influence of that parameter on  $L/H_{crit}$ . The systematic tests (from the first step) could be  
178 used to ensure that the extremes of the parameter ranges have been sampled and to ensure confidence  
179 in our assertion about the maximum  $L/H$  ratio required to satisfy the infinite slope assumptions. Both  
180 the systematic and Monte Carlo explorations involved modifying the parameters in combination (as  
181 opposed to one at a time) to account for interaction effects between parameters.

182  
183 <Table 1 near here>

184  
185 **Finite Element method**

186 To benchmark the infinite slope predictions for slopes of a defined length, we compare them with a  
187 finite element method developed by Griffiths and Lane (1999) and modified by Griffiths *et al.*  
188 (2011) to make it suitable for landslides on long slopes with very high  $L/H$  ratios. The method has  
189 been validated against the infinite slope method for scenarios where the FE domain simulates infinite

length conditions (Griffiths *et al.*, 2011, Sections 4 and 5). The model performs 2D plane strain analysis of elastic-perfectly plastic soils with a Mohr-Coulomb failure criterion using 8-node quadrilateral elements with reduced integration (4 Gauss-points per element) in the gravity loads generation, the stiffness matrix generation and the stress redistribution phases of the algorithm. The soil is initially assumed to be elastic and the model generates normal and shear stresses at all Gauss-points within the mesh. These stresses are then compared with the Mohr-Coulomb failure criterion. If the stresses at a particular Gauss-point lie within the Mohr-Coulomb failure envelope then that location is assumed to remain elastic. If the stresses lie on or outside the failure envelope, then that location is assumed to be yielding. Yield stresses are redistributed throughout the mesh using the visco-plastic algorithm (Perzyna 1966, Zienkiewicz *et al.* 1975). Overall shear failure occurs when a sufficient number of Gauss-points have yielded to allow a mechanism to develop. The factor of safety is defined as the ratio of the average shear strength of the soil to the average shear stress developed along the critical failure surface and is calculated using the shear strength reduction technique (Zienkiewicz *et al.*, 1975).

The domain geometry and boundary conditions are designed to represent slopes of a finite length. They should be simple enough to isolate the effect of length on stability but representative so that we can be confident that our conclusions apply to natural slopes. We use a mesh of 8-noded quadrilateral elements (shown in Figure 3). The mesh consists of horizontal sections to the left and right, and a long sloping central section. The base of the mesh is fully fixed and the extreme vertical boundaries to the left and right allow vertical movement only. This simple representation of a finite slope, with a sloping section between two horizontal sections, is common in slope stability modelling (Chugh, 2003). The boundary conditions on the base are exactly the same as in the IS method in that shearing can occur at the base of the soil layer. We chose fixed rather than periodic vertical boundaries since we are interested in the IS method's ability to represent finite slopes. We added horizontal sections 4 times the domain depth and allowed vertical movement on the vertical boundaries to minimize edge effects. The size of real landslides is defined not only by a slope's geometry but also its pore water pressure and material properties, which vary across the slope. This

1 218 variability might be responsible for defining the unstable part of a slope but cannot be represented  
2 219 within the IS method. The simplest way of creating a zone of decreased stability between two more  
3  
4 220 stable zones is to change the domain geometry at the head and toe. In this respect we are changing  
5  
6 221 the geometry to create more stable regions and ensure that the failure is a finite (defined) length. We  
7  
8 222 tested end sections inclined at a range of angles but found that for sloping end sections the failure  
9  
10 223 can expand to fill the full domain. This increases the influence of the vertical boundary conditions  
11  
12 224 and alters the geometry of the failure plane so that it is no longer consistent with the IS method. We  
13  
14 225 chose horizontal sections for consistency and simplicity. This represents both the specific case of a  
15  
16 226 finite slope with uniform material properties and horizontal sections above and below it and the more  
17  
18 227 general case of a slope with more stable zones above and below it. Our tests using a sloping end  
19  
20 228 sections showed that where the failure was limited to the sloping section change in inclination of the  
21  
22 229 end sections lead to only minor changes in predicted stability.  
23  
24  
25  
26  
27  
28

29 230  
30  
31 231 <Figure 3 near here>  
32

33 232  
34  
35 233 We represent the slope geometry and soil properties using the six parameters shown in Table 1 with  
36  
37 234 elastic parameters Young's modulus and Poisson's ratio, which are needed by the displacement-  
38  
39 235 based FE formulation to introduce stresses into the model. These elastic parameters have been shown  
40  
41 236 to have little influence on stability predictions (Hammah *et al.*, 2005) and are held constant  
42  
43 237 throughout the study at nominal values of  $10^5$  kPa and 0.3 respectively.  
44  
45 238

46  
47 239 The FE model has one further soil parameter, the dilation angle, which affects the volume change of  
48  
49 240 the soil during yielding. It is well known that the actual volume change exhibited by a soil during  
50  
51 241 yielding is quite variable. For example a medium dense material during shearing might initially  
52  
53 242 exhibit some volume decrease ( $\psi < 0$ ) followed by a dilative phase ( $\psi > 0$ ), leading eventually to  
54  
55 243 yield under constant volume conditions ( $\psi = 0$ ). Clearly this type of detailed volumetric modelling is  
56  
57 244 beyond the scope of the elastic-perfectly plastic models used in this study where a constant dilation  
58  
59 245 angle is implied. The question then arises as to what value of  $\psi$  to use. If  $\psi = \phi$  then the plasticity

flow rule is 'associated' and direct comparisons with theorems from classical plasticity can be made. In spite of this potential advantage, it is also well known that associated flow rules with frictional soil models predict far greater dilation than is ever observed in reality. This in turn leads to increased failure load prediction, especially in confined problems such as bearing capacity (e.g. Griffiths 1982). Slope stability analysis, especially with long slopes, is relatively unconfined, thus the choice of dilation angle is less important (Griffiths and Marquez, 2007). As the main objective of the current study is the accurate prediction of slope factors of safety, a compromise value of  $\psi = 0$ , corresponding to a non-associated flow rule with zero volume change during yield, has been used throughout this paper. This value of  $\psi$  enables the model to give reliable factors of safety and a reasonable indication of the location and shape of the potential failure surfaces.

## Results

### *Systematic parameter exploration*

For a given slope geometry and set of material properties Figure 4a shows that the *FoS* predicted by the FE method at a  $L/H$  ratio of 2 is very high, almost double the IS *FoS*. The *FoS* predictions from the FE method decline steeply as the  $L/H$  ratio increases, so that the IS predictions are within 10% of the FE prediction for  $L/H$  ratios greater than 10 and within 5 % for  $L/H$  ratios greater than 12. The FE predictions asymptote at the IS *FoS*. We can use the difference between the FE and IS methods at any given  $L/H$  ratio as an indicator of the error in the IS method resulting from the assumption of infinite length. We can then use the length at which the IS method predictions fall within 5 or 10% of the FE predictions to calculate a critical  $L/H$  ratio ( $L/H_{crit}$ ) at which the assumption of infinite length can be considered reasonable. However, we need to know how general this result is under the range of plausible conditions and which other properties of the slope exert a controlling influence on  $L/H_{crit}$ . The systematic parameter exploration provides the data required to address these questions and can most easily be visualised by calculating the difference between IS and FE predictions across the range of  $L/H$  ratios then normalising this difference as a percentage of the FE *FoS*. The resultant curves are shown in Figure 4b for the unsaturated cases.

273

274 <Figure 4 near here>

275

276 During the systematic parameter exploration, cohesion appeared to exert the strongest control on the

277 *FoS* difference curves and on the  $L/H_{crit}$  value. In fact when cohesion was set to zero the FE

278 predictions did not fall outside 10% of the IS predictions even at the shortest  $L/H$  ratio (4).

279 Examining the deformed post failure mesh for cohesionless soils within the FE method revealed that

280 they fail in the top layer of elements (Figure 5a). This result fits closely with the IS method for

281 cohesionless soils, which assumes that failure is equally likely at all depths. In this case we would

282 expect failure at an infinitely shallow depth where the additional reinforcement at the toe would be

283 least, the length / depth ratio would be infinite and the infinite length assumption would be most

284 completely fulfilled. In the FE scheme, failure at an infinitely small depth would be represented as

285 failure in the top layer of elements (Figure 5a) but this makes the results difficult to interpret in terms

286 of critical  $L/H$  values since in this case  $L/H$  will always be infinite independent of the domain

287 dimensions and any departure from this will be a function of the discretisation of the domain. As a

288 result, we modified our sampling to sample three further cohesions: a negligible but non zero

289 cohesion (0.1 kPa); a very low cohesion (1 kPa) and a midpoint between the two previous cohesion

290 limits (10 kPa).

291

292 <Figure 5 near here>

293

294 Increasing cohesion slightly to 0.1 kPa forces the failure plane down below the first row of elements

295 (Figure 5b) but not always to the full depth of the model domain. In this situation the FE method

296 captures the competing effects of: additional downslope driving force with depth (represented in the

297 IS method); but also additional reinforcement with depth at the downslope margin of the landslide.

298 As a result, the FE model's failure plane depth differs from the IS prediction, which is always at the

299 base of the domain for cohesive soils. These FE model runs provide reliable  $L/H_{crit}$  predictions that

300 are often very small (Figure 4b), immediately suggesting that the  $L/H_{crit}$  value provided by Griffiths

301 *et al.* (2011) is only one example of a range of possible values and that varying slope properties leads  
 302 to different  $L/H_{crit}$  values.  
 303  
 304 Increasing the cohesion further to 1 kPa we find that the failure plane is now forced down to the base  
 305 of the model domain (Figure 5c). For these slope properties the curve is much steeper and more  
 306 similar to the results reported by Griffiths *et al.* (2011) (Figure 4b). Further increases in cohesion, to  
 307 10 kPa (a relatively high value for colluvial soils; see Hammond *et al.*, 1992), result in only small  
 308 changes to the form of the failure (Figure 5d) and to the  $L/H_{crit}$  value (Figure 4b). Figure 4b shows  
 309 the form of the *FoS* difference curves at the limits of the slope properties but is difficult to interpret  
 310 in terms of the influence of individual parameters on the  $L/H_{crit}$  value because: 1) it only shows  
 311 results for the extremes; and 2) the parameter combinations are difficult to differentiate. We address  
 312 these limitations using the random parameter exploration.

313

### 314 ***Random Parameter Exploration***

315 The results from the random parameter exploration are displayed as a series of scatter plots in Figure  
 316 6. The patterns for each parameter are similar for convergence at 5 and 10% thresholds but with a  
 317 lower maximum  $L/H_{crit}$  value for the 10% than the 5% threshold. They show that for almost all  
 318 parameter combinations the IS predictions converge to within 5 and 10% of those from the FE  
 319 method at  $L/H$  ratios of no more than 25 and 18 respectively.

320

321 <Figure 6 near here>

322

323 Of the six infinite slope parameters  $L/H_{crit}$  appears most sensitive to slope angle, with a strong  
 324 negative trend to the upper  $L/H_{crit}$  limit with slope.  $L/H_{crit}$  is also sensitive to, soil depth, normalised  
 325 free surface height and friction angle. There are strong negative trends to the upper  $L/H_{crit}$  limit for,  
 326 friction angle and soil depth and nonlinear negative trends to the lower  $L/H_{crit}$  limit for soil depth and  
 327 normalised free surface height so that low  $L/H_{crit}$  values are only possible for soils deeper than 1 m

and normalised free surface heights greater than 0.2. Increasing cohesion from very low values causes a rapid nonlinear increase in the upper  $L/H_{crit}$  limit. The highest  $L/H_{crit}$  values are associated with high cohesion; and low soil depth, slope angle and friction angle; the lowest  $L/H_{crit}$  values are associated with low cohesion; and high soil depth, normalised free surface height and slope angle.

**Discussion**

***Critical length depth ratio***

Both the systematic and random parameter explorations confirm that the  $FoS$  predictions from the FE method converge on those of the IS method across the full range of slope properties and geometries that we might find in a catchment. The critical length depth ratio ( $L/H_{crit}$ ) at which the FE predictions converge to within 5 or 10% of the IS predictions varies with friction angle, cohesion, soil depth, normalised free surface height and slope angle but is insensitive to soil unit weight. For a 5% threshold,  $L/H_{crit}$  values can range from 4 (effectively the detection limit for our study) to 25 and for a 10% threshold they vary from 4 to 18.

Slope angle appears the dominant control on the upper limit to  $L/H_{crit}$  values. This is perhaps unsurprising given that our definitions of length and depth are planimetric and vertical respectively. As slope angle ( $\beta$ ) increases the true length ( $L_t$ ) increases relative to the planimetric length ( $L_p$ ) according to:  $L_p = L_t / \cos(\beta)$  while the true (slope perpendicular) depth ( $H_t$ ) decreases relative to the vertical depth ( $H_v$ ) according to:  $H_t = H_v / \cos(\beta)$ . As a result the true length depth ratio ( $L_t/H_t$ ) is related to the planimetric length depth ratio ( $L_p/H_v$ ) according to  $L_t/H_t = L_p/H_v (1/\cos^2(\beta))$ . The decrease in  $L/H_{crit}$  with slope angle closely follows the expected decrease resulting from this difference between true and planimetric dimensions (grey lines in Figure 6). Despite this, we have continued to use planimetric lengths and vertical depths since these are the dimensions commonly used within catchment slope stability models. Much of the remaining variability is related to the proportion of the soil strength made up by cohesion. We know from Figure 4 and Figure 5 that the lowest  $L/H_{crit}$  values will always be found in cohesionless soils; and from Figure 6 that shallow soils

with high cohesion have higher  $L/H_{crit}$  values. However, even the steep ( $>30^\circ$ ), shallow ( $<1$  m), low cohesion ( $<5$  kPa) and high friction ( $>30^\circ$ ) soils commonly found in upland catchments show a relatively broad range of  $L/H_{crit}$  values (5-15 at 10% and 5-20 at 5%). With generalisation to all site properties considered the infinite length assumption within the IS method results in errors of less than 10% for  $L/H$  ratios greater than 18 and less than 5% for  $L/H$  ratios greater than 25 (Figure 6). This has important implications for slope stability modelling using the infinite slope method and we will explore these in detail in the following section.

### ***Implications for geomorphic and landscape evolution models***

Catchment landslide models solve the infinite slope equation for each cell in a mesh. They assume implicitly that the (downslope) length and (across slope) width of these cells represent the dimensions of the predicted landslide (Dietrich *et al.*, 2008) and that these dimensions are large enough relative to the failure plane that the infinite slope assumption is valid (Ray *et al.*, 2010). Our results suggest that the infinite length assumption is valid, and results in less than 5% error for landslides (and therefore model cells) with  $L/H$  ratios greater than 25 independent of material properties. This validity will hold provided the grid resolution is more than 25 times the expected failure plane depth. For example, many studies use a spatially constant failure plane depth of  $\sim 1$  m (e.g. Montgomery and Deitrich, 1994; Wu and Sidle, 1995). In this case, models with a grid resolution of 25 m or more can apply the infinite slope method without significant length effects. However, for models with a cell size less than 25 times the assumed landslide failure plane depth, edge effects become possible and are likely to be significant if the length / depth ratio drops below 8. In these cases many of the IS predictions differed from the FE predictions by greater than 50%. Assuming failures of equal length and width, with a 1 m depth, this would mean that even groups of  $\sim 60$  1 m resolution cells are likely to be predicted as 50% less stable than they should be as a result of length effects not represented by the infinite slope method. The dependence of the validity of the infinite slope model upon cell size emphasises that care is required in assuming that higher resolution topographic data always improve identification of landslide risk. Although the coarser cell



1 382 size may result in error because of the minimum landslide area that can be identified, higher  
2 383 resolution data may result in error since the identified landslides may violate the infinite slope length  
3  
4 384 assumption.  
5  
6 385  
7  
8  
9 386 To demonstrate the implications that this has for a catchment scale stability model we applied a  
10  
11 387 simple grid based stability model, using photogrammetrically derived topographic data (Milledge *et*  
12  
13 388 *al.*, 2009), to produce a set of predicted landslides for a 1 km<sup>2</sup> study area in the English Lake  
14  
15 389 District, Northern England (Warburton, *et al.* 2008). As we have discussed above, the main  
16  
17 390 difference in catchment scale stability models is the hydrological treatment used to define the pore  
18  
19 391 water pressure field. There is considerable debate around what drives the pore water pressure  
20  
21 392 increase that triggers landslides, with different groups arguing that it is: dominated by lateral  
22  
23 393 redistribution of water (e.g. Montgomery and Dietrich 1994; 2004; Montgomery *et al.*, 2002);  
24  
25 394 dominated by vertical infiltration (e.g. Iverson, 2000; 2004); or a combination of these (e.g.  
26  
27 395 D’Odorico and Fagherazzi, 2003). We will give an example for the simple and widely used case  
28  
29 396 where the pore water pressure field is driven by lateral redistribution. To do this we applied  
30  
31 397 SHALSTAB (Dietrich and Montgomery, 1998) in a deterministic sense (i.e. for a defined rainfall  
32  
33 398 and transmissivity). This model setup is analogous to the stability treatment within those landscape  
34  
35 399 evolution models that attempt to model hydrologically triggered landslides (e.g. Tucker and Bras,  
36  
37 400 1998). While it is very simple, its basis around the topographic control on spatial soil moisture is  
38  
39 401 very common (e.g. Wu and Sidle, 1995; Burton and Bathurst, 1998; Pack *et al.*, 1998; Borga *et al.*,  
40  
41 402 2002; Vanacker *et al.*, 2003; Dhakal and Sidle, 2004; Reid *et al.*, 2007; Simoni *et al.*, 2008; for  
42  
43 403 exceptions see: Iverson, 2000; Baum *et al.*, 2008).  
44  
45 404  
46  
47  
48  
49  
50  
51 405 We ran the model to predict landslides in two different scenarios: 1) the most common scenario,  
52  
53 406 using a coarse (10 m) grid resolution since this is a resolution typical of the most widely available  
54  
55 407 topographic data; and 2) the increasingly common scenario of finer (1 m) grid resolution to take  
56  
57 408 advantage of the constantly improving topographic data.  
58  
59 409  
60

1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

410 <Figure 7 near here>

411

412 Existing research has highlighted the influence of grid resolution on this type of model (e.g. Dietrich  
413 and Montgomery, 1998; Claessens *et al.*, 2005). Our predicted landslides have characteristics that  
414 are consistent with previous findings, particularly that new areas of potential instability are identified  
415 at finer resolution (e.g. upper left corner of the Figure 7b). These relate to improved topographic  
416 representation, which captures small steep areas that were previously smoothed out at the coarser  
417 resolution. We also find that many of the predicted landslides are long for both the high and low  
418 resolution model runs. The hydrological model generates patches of high pore water pressure that are  
419 long in a downslope direction. As a result the model predicts long landslides and with high  $L/H$   
420 ratios that minimise the error associated with using the IS method. This suggests that the IS method  
421 can applied in this case with high resolution data without violating its infinite length assumption. It is  
422 worth noting that these long zones of predicted instability are a function of the model's assumption  
423 that lateral redistribution drives pore water pressure patterns. It is the underlying hydrological  
424 processes that drive characteristic  $L/H$  ratios; and these produce slides with  $L/H$  ratios that do not  
425 violate the infinite slope stability assumption in this case. This suggests that the acceptability of the  
426 IS model depends not only on data resolution but also on catchment hydrology and its representation  
427 in the landslide model. Models with different hydrological representation might produce zones of  
428 instability with different geometries, although lateral redistribution remains important control  
429 through its influence on antecedent pore water pressures (Iverson, 2000; Montgomery and Dietrich,  
430 2004). The suitability of these models will need to be assessed with reference to our findings on the  
431 critical  $L/H$  ratio at which the IS method becomes applicable. Critically, our results do not give a  
432 single answer on the suitability of the IS method for geomorphological slope stability modelling, but  
433 they provide a tool to assess its suitability on a case by case basis, something that should be a routine  
434 part of testing these models.

435

436 While finer grid resolutions still predict long landslides the predicted width is dramatically reduced.  
437 This prompts an important question: how reasonable is the assumption of infinite width and what are

1 438 the critical width depth ratios at which the infinite slope assumptions break down? This question  
2 439 cannot be addressed using the 2D finite element geotechnical model used in this study, since it also  
3  
4 440 assumes a slope of infinite width. Instead, solving this question would require a similar research  
5  
6 441 design within a 3D model, such models exist and research to address this question is underway.  
7  
8  
9 442

10  
11  
12 443 **Conclusion**  
13

14  
15 444 Factor of safety predictions from the Finite Element method always converge to within 5 % of those  
16  
17 445 from the infinite slope method when the length / depth ratio exceeds 25. However, they can converge  
18  
19 446 at much lower length / depth ratios depending on the geometry and material properties of the slope.  
20  
21 447 The critical length depth ratio at which the predictions converge is in part controlled by the  
22  
23 448 proportion of the soil strength that comes from cohesion rather than from friction with the longer  
24  
25 449 length depth ratios required for more cohesive soils and very rapid convergence at low length depth  
26  
27  
28 450 ratios for low cohesion soils.  
29

30  
31 451  
32  
33 452 The infinite length assumption within the infinite slope method is valid for many of the existing  
34  
35 453 modelling studies, which have used a coarse (>25 m) resolution. For models with a finer resolution  
36  
37 454 (<10 m) the assumption of infinite length might be less valid depending on the assumed landslide  
38  
39 455 failure plane depth and on the material properties. However, if lateral subsurface flow plays a role in  
40  
41 456 defining pore water pressure then its spatial organisation mitigates against predicting short landslides  
42  
43 457 and minimises the risk that predicted landslides will have length depth ratios less than 25.  
44  
45

46 458  
47  
48 459 In this case, whilst it is unlikely that the infinite length assumption introduces error into the stability  
49  
50 460 predictions because modelled landslides are often long, the infinite width assumption is more likely  
51  
52 461 to be violated since predicted landslides get narrower as the grid resolution is reduced. It may be  
53  
54 462 width and not length that limits the applicability of the infinite slope method and maintains the  
55  
56 463 stability of potential landslides. This is a topic that requires further research since it is not tractable  
57  
58 464 within a standard 2D geotechnical profile treatment but requires a 3D approach.  
59  
60

465

## 466 Acknowledgements

467 Data used as part of this research were funded by NERC Research Grant NE/D521481/1 to JW.  
468 DGM was funded by NERC PhD Studentship NER/S/A/2004/12248 and NERC Fellowship  
469 NE/H015949/1.

470

## 471 References

- 472 Bathurst JC, Moretti G, El-Hames A, Moaven-Hashemi A, Burton A. 2005. Scenario modelling of  
473 basin-scale, shallow landslide sediment yield, Valsassina, Italian Southern Alps. *Natural Hazards*  
474 *and Earth System Sciences* **5**: 189-202.
- 475 Baum RL, Savage WZ, Godt JW. 2008. TRIGRS - a fortran program for transient rainfall infiltration  
476 and grid-based regional slope stability analysis, version 2.0. In, *Open File Report* (p. 81): U.S.  
477 Geological Survey.
- 478 Borga M, Dalla Fontana G, Gregoretti C, Marchi L. 2002. Assessment of shallow landsliding by  
479 using a physically based model of hillslope stability. *Hydrological Processes* **16**: 2833-2851.
- 480 Burton A, Bathurst JC. 1998. Physically based modelling of shallow landslide sediment yield at a  
481 catchment scale. *Environmental Geology* **35**: 89-99.
- 482 Casadei M, Dietrich WE, Miller NL. 2003. Testing a model for predicting the timing and location of  
483 shallow landslide initiation in soil-mantled landscapes. *Earth Surface Processes and Landforms* **28**:  
484 925-950.
- 485 Chugh AK. 2003. On the boundary conditions in slope stability analysis. *International Journal for*  
486 *Numerical and Analytical Methods in Geomechanics* **27**: 905-926.
- 487 Claessens L, Heuvelink GBM, Schoorl JM, Veldkamp A. 2005. DEM resolution effects on shallow  
488 landslide hazard and soil redistribution modelling. *Earth Surface Processes and Landforms* **30(4)**:  
489 461-477, doi: 10.1002/esp.1155

1 490 Crosta GB, Frattini P. 2003. Distributed modelling of shallow landslides triggered by intense  
2 491 rainfall. *Nat. Hazards Earth Syst. Sci.* **3**: 81-93.  
3  
4 492 Dhakal AS, Sidle RC. 2004. Distributed simulations of landslides for different rainfall conditions.  
5  
6 493 *Hydrological Processes* **18**: 757-776.  
7  
8 494 Dietrich WE, McKean J, Bellugi D, Perron T. 2008. The prediction of shallow landslide location and  
9  
10 495 size using a multidimensional landslide analysis in a digital terrain model. In *Fourth International*  
11  
12 496 *Conference on Debris-Flow Hazards Mitigation: Mechanics, Prediction, and Assessment (DFHM-*  
13  
14 497 *4), Chengdu, China, September 10-13, 2007*, Chen CL, Major JJ (eds). Amsterdam: IOS Press.  
15  
16 498 Dietrich WE, Montgomery DR. 1998. SHALSTAB: a digital terrain model for mapping shallow  
17  
18 499 landslide potential. In, *Technical Report* (p. 29): NCASI.  
19  
20 500 D'Odorico P, Fagherazzi S. 2003. A probabilistic model of rainfall-triggered shallow landslides in  
21  
22 501 hollows: A long-term analysis, *Water Resources Research*. **39**: 1262, doi:10.1029/2002WR001595.  
23  
24 502 Gabet EJ, Dunne T. 2002. Landslides on coastal sage-scrub and grassland hillslopes in a severe El  
25  
26 503 Nino winter: The effects of vegetation conversion on sediment delivery. *Geological Society of*  
27  
28 504 *America Bulletin* **114**: 983-990.  
29  
30 505 Griffiths DV. 1982. Computation of bearing capacity factors using finite elements. *Geotechnique*  
31  
32 506 **32(3)**: 195-202.  
33  
34 507 Griffiths DV, Huang JS, Dewolfe GF. 2011. Numerical and analytical observations on long and  
35  
36 508 infinite slopes. *International Journal for Numerical and Analytical Methods in Geomechanics* **35**:  
37  
38 509 569-585.  
39  
40 510 Griffiths DV, Lane PA. 1999. Slope stability analysis by finite elements. *Geotechnique* **49**: 387-403.  
41  
42 511 Griffiths DV, Marquez RM. 2007. Three-dimensional slope stability analysis by elasto-plastic finite  
43  
44 512 elements. *Geotechnique* **57**: 537-546.  
45  
46 513 Haefeli R. 1948. The stability of slopes acted upon by parallel seepage. In *International Conference*  
47  
48 514 *on Soil Mechanics and Foundation Engineering*; 57-62.  
49  
50 515 Hammah RE, Yacoub TE, Corkum B, Curran JH. 2005. A comparison of finite element slope  
51  
52 516 stability analysis with conventional limit-equilibrium investigation. In *58th Canadian Geotechnical*  
53  
54  
55  
56  
57  
58  
59  
60

- 517 and 6th Joint IAH-CNC and CGS Groundwater Specialty Conferences - GeoSask 2005. Saskatoon;  
518 480-487.
- 519 Haneberg WC. 2004. A rational probabilistic method for spatially distributed landslide hazard  
520 assessment. *Environmental & Engineering Geoscience* **10**: 27-43.
- 521 Iverson RM. 2000. Landslide triggering by rain infiltration. *Water Resources Research* **36**: 1897-  
522 1910.
- 523 Iverson RM. 2004. Comment on “Piezometric response in shallow bedrock at CB1: Implications for  
524 runoff generation and landsliding” by David R. Montgomery, William E. Dietrich, and John T.  
525 Heffner, *Water Resources Research* **40**: W03801, doi:10.1029/2003WR002077.
- 526 Larsen IJ, Montgomery DR, Korup O. 2010. Landslide erosion controlled by hillslope material.  
527 *Nature Geosci* **3**: 247-251.
- 528 Milledge DG. 2009. Digital filtering of generic topographic data in geomorphological research.  
529 *Earth Surface Processes and Landforms* **34**: 63-74.
- 530 Montgomery DR, Dietrich WE. 1994. A Physically-Based Model for the Topographic Control on  
531 Shallow Landsliding. *Water Resources Research* **30**: 1153-1171.
- 532 Montgomery DR, Dietrich WE, Heffner JT. 2002. Piezometric response in shallow bedrock at CB1:  
533 Implications for runoff generation and landsliding, *Water Resources Research*. **38**(12): 1274,  
534 doi:10.1029/ 2002WR001429.
- 535 Montgomery DR, Dietrich WE. 2004. Reply to comment by Richard M. Iverson on “Piezometric  
536 response in shallow bedrock at CB1: Implications for runoff generation and landsliding,” *Water*  
537 *Resources Research* **40**: W03802, doi:10.1029/2003WR002815.
- 538 Pack RT, Tarboton DG, Goodwin CN. 1998. The SINMAP approach to terrain stability mapping In,  
539 *8th International Congress of the International Association for Engineering Geology and the*  
540 *Environment*. Vancouver, Canada.
- 541 Perzyna P. 1966. Fundamental problems in viscoplasticity. *Advances in Applied Mechanics* **9**: 243–  
542 377.

1 543 Ray RL, Jacobs JM, de Alba P. 2010. Impacts of Unsaturated Zone Soil Moisture and Groundwater  
2 544 Table on Slope Instability. *Journal of Geotechnical and Geoenvironmental Engineering* **136**: 1448-  
3 545 1458.  
4  
5  
6 546 Reid SC, Lane SN, Montgomery DR, Brookes CJ. 2007. Does hydrological connectivity improve  
7  
8 547 modelling of coarse sediment delivery in upland environments? *Geomorphology* **90**: 263-282.  
9  
10 548 Simoni S, Zanotti G, Bertoldi G, Rigon R. 2008. Modelling the probability of occurrence of shallow  
11  
12 549 landslides and channelized debris flows using GEOtop-FS. *Hydrological Processes* **22**: 2248-2263.  
13  
14 550 Skempton AW, DeLory FA. 1957. Stability of natural slopes in London clay. In *4th International*  
15  
16 551 *Conference on Soil Mechanics and Foundation Engineering*; 378-381.  
17  
18 552 Taylor DW. 1948. *Fundamentals of Soil Mechanics*. Wiley: New York.  
19  
20 553 Tucker GE, Bras RL. 1998. Hillslope processes, drainage density, and landscape morphology. *Water*  
21  
22 554 *Resources Research* **34**: 2751-2764.  
23  
24 555 Vanacker V, Vanderschaeghe M, Govers G, Willems E, Poesen J, Deckers J, De Bievre B. 2003.  
25  
26 556 Linking hydrological, infinite slope stability and land-use change models through GIS for assessing  
27  
28 557 the impact of deforestation on slope stability in high Andean watersheds *Geomorphology* **52**: 299-  
29  
30 558 315.  
31  
32 559 Warburton J, Milledge DG, Johnson RM. 2008. Assessment of shallow landslide activity following  
33  
34 560 the January 2005 storm, Northern Cumbria. *Proceedings of the Cumberland Geological Society* **7**:  
35  
36 561 263-283.  
37  
38 562 Wu WM, Sidle RC. 1995. A Distributed Slope Stability Model for Steep Forested Basins. *Water*  
39  
40 563 *Resources Research* **31**: 2097-2110.  
41  
42 564 Zienkiewicz OC, Humpheson C, Lewis RW. 1975. Associated and Non-Associated Visco-Plasticity  
43  
44 565 and Plasticity in Soil Mechanics. *Geotechnique* **25**: 671-689.  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

## Tables

**Table 1: Parameters varied within the parameter exploration with the range over which they were varied. Young's Modulus and Poisson's Ratio were held constant at the values below.**

Parameter	Value Range
Friction Angle ( $\phi'$ )	15 - 45°
Cohesion ( $c'$ )	0 - 20 kPa
Soil Depth ( $H$ )	0 - 3 m
Normalised free surface height ( $m$ )	0 - 1
Soil Unit Weight ( $\gamma_{sat}$ )	1.1 - 1.8 kN m <sup>-3</sup>
Slope Angle ( $\beta$ )	15 - 45°
Young's Modulus	10 <sup>5</sup> kPa
Poisson's Ratio	0.3

## Figures

**Figure 1: Cumulative probability distributions for the length / depth ratios of landslides from two inventories in Cumbria, UK (Warburton *et al.*, 2008) and and California, USA (Gabet and Dunne, 2003).**

**Figure 2: Schematic profile view through an infinite slope showing the relevant forces and lengths.**

**Figure 3: example finite element mesh of 8-node quadrilateral elements annotated to show the relevant lengths and angles used within the model.**

**Figure 4: A) relationship between length / depth ratio and factor of safety for infinite slope (IS) and finite element (FE) models for an example slope with  $\phi'=30^\circ$ ,  $c'=20$  kPa,  $\gamma_{sat}=19$  kN m<sup>-3</sup>,  $H=5$  m and  $\beta=25^\circ$ ; B) difference between FE and IS predictions (expressed as a percentage of FE  $FoS$ ) for different length / depth ratios.**

**Figure 5: deformed meshes showing the shape of the failure mechanism for a slope with  $\phi'=20^\circ$ ,  $\gamma_{sat}=1.9$  kN m<sup>-3</sup>,  $m=0$ ,  $L=2$  m,  $H=0.5$  m,  $\beta=20^\circ$  and cohesions of: A) 0 kPa, B) 0.1 kPa, C) 1 kPa, and D) 10 kPa. Displacements are exaggerated for visualisation and should be interpreted as relative rather than absolute.**

**Figure 6: uncertainty plots showing variation in the length / depth ratio at which the infinite slope predictions converge to within 5 and 10% of the finite element predictions ( $L/H_{crit}$ ) for a range of: friction angles, soil cohesions, soil depths, normalised free surface heights, soil unit weights and slope angles. The bottom row shows results for parameters sampled to zero in semi-logarithmic space to illustrate their influence at low values. The grey lines on the slope angle plots have the equation  $y = a \cos^2(\beta)$ , where  $a = 24$  and  $16$  for the upper and lower plots respectively.**

**Figure 7: predicted landslides from a 1 km<sup>2</sup> patch of a grid based stability model with  $\phi'=40^\circ$ ,  $c'=1$  kPa,  $\gamma_{sat}=1.7$  kN m<sup>-3</sup>, transmissivity = 0.01 mm h<sup>-1</sup> and steady state rainfall rate = 100 mm h<sup>-1</sup>,  $H=1$  m, cellsize is 10 m for a and 1 m for b.**



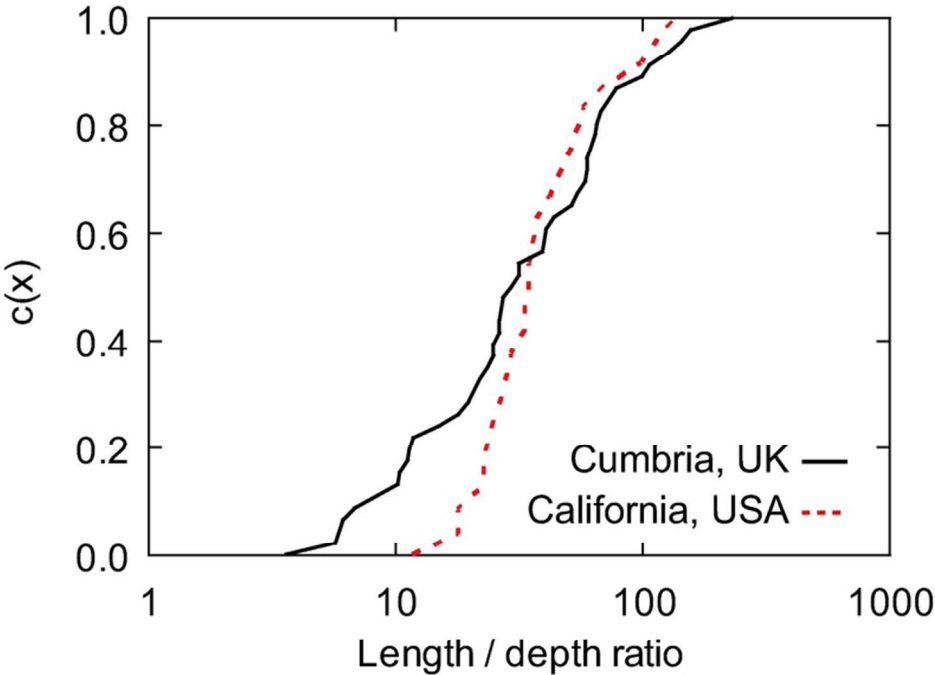


Figure 1: Cumulative probability distributions for the length / depth ratios of landslides from two inventories in Cumbria, UK (Warburton et al., 2008) and California, USA (Gabet and Dunne, 2003).  
71x55mm (300 x 300 DPI)

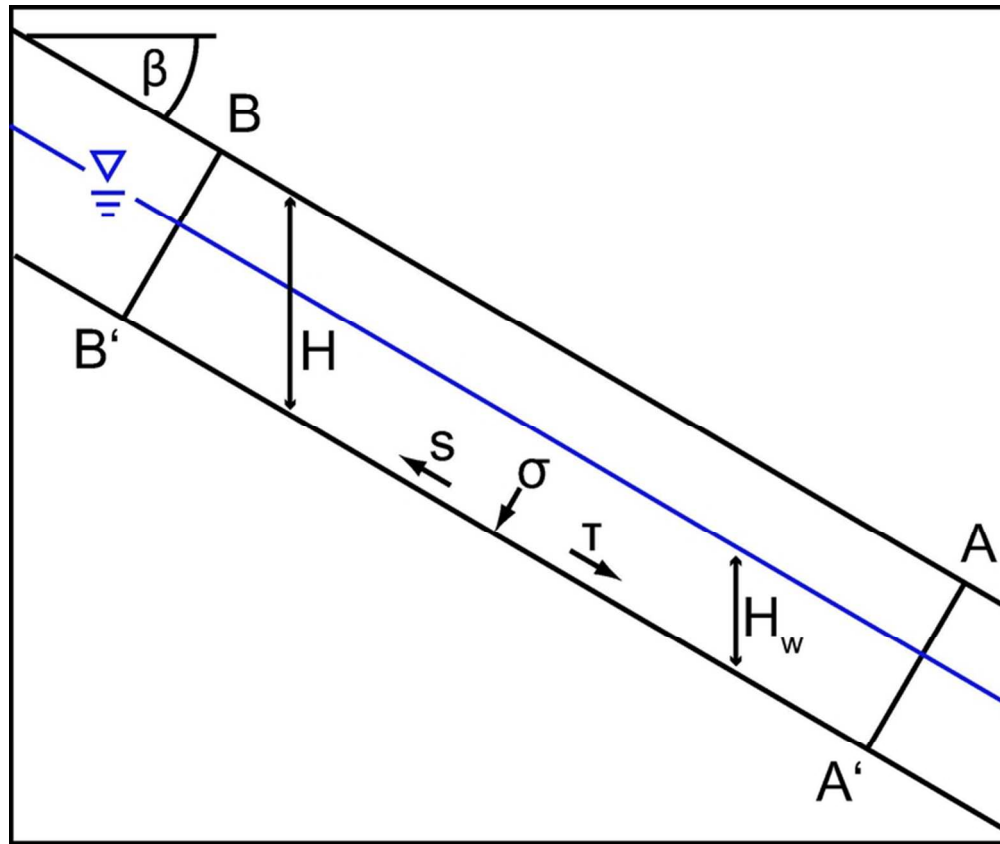


Figure 2: Schematic profile view through an infinite slope showing the relevant forces and lengths.  
65x55mm (300 x 300 DPI)

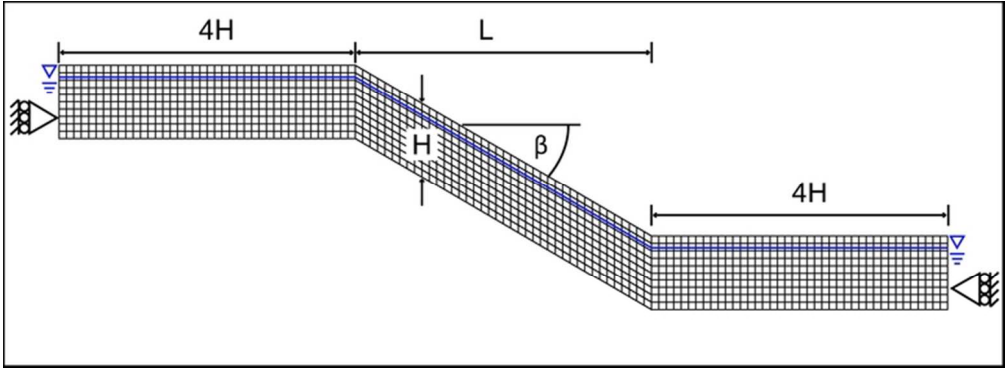


Figure 3: example finite element mesh of 8-node quadrilateral elements annotated to show the relevant lengths and angles used within the model.  
65x24mm (300 x 300 DPI)

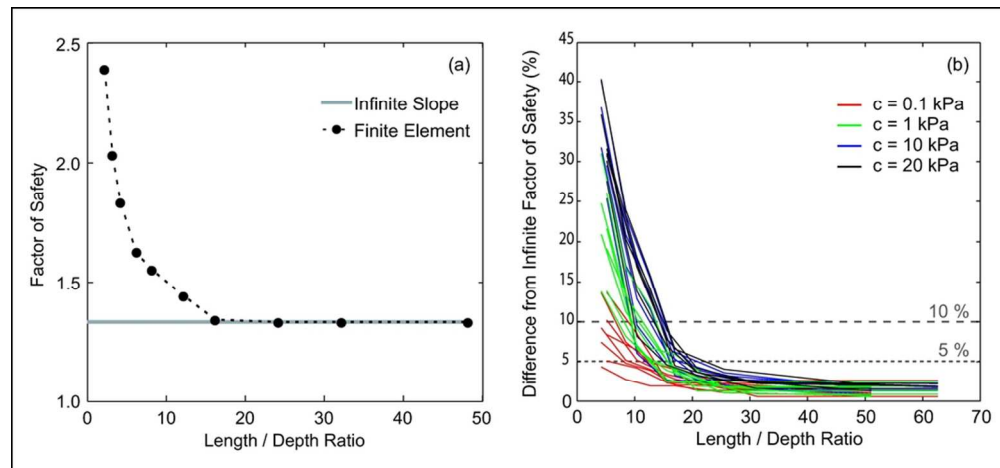


Figure 4: A) relationship between length / depth ratio and factor of safety for infinite slope (IS) and finite element (FE) models for an example slope with  $\phi' = 30^\circ$ ,  $c' = 20$  kPa,  $\gamma_{\text{sat}} = 19$  kN m<sup>3</sup>,  $H = 5$  m and  $\beta = 25^\circ$ ; B) difference between FE and IS predictions (expressed as a percentage of FE FoS) for different length / depth ratios.

90x42mm (300 x 300 DPI)

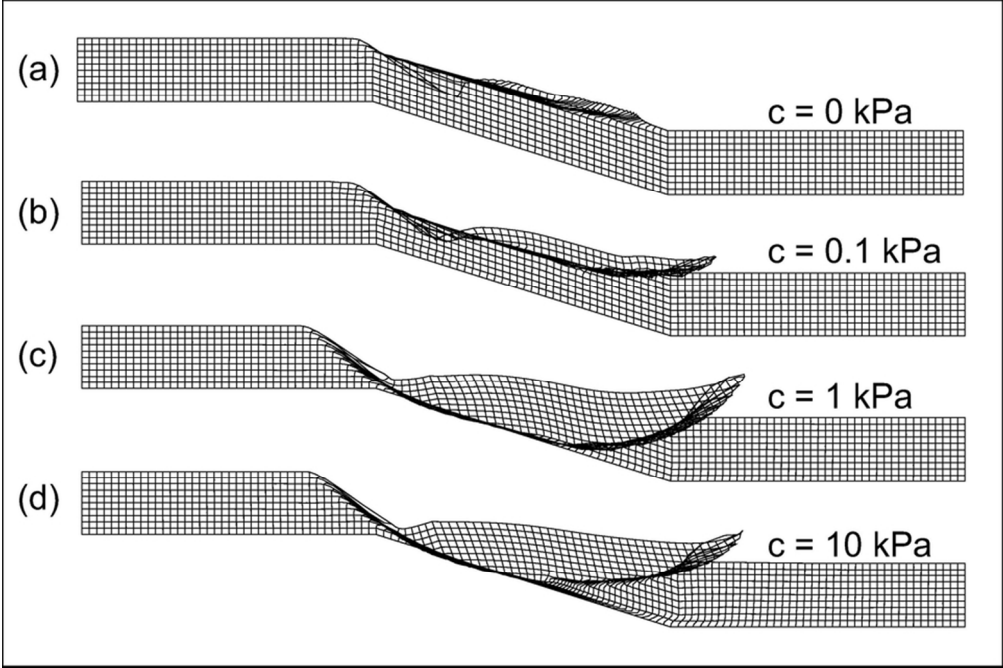


Figure 5: deformed meshes showing the shape of the failure mechanism for a slope with  $\phi'=20^\circ$ ,  $\gamma_{\text{sat}}=1.9\text{kN m}^{-3}$ ,  $m = 0$ ,  $L = 2 \text{ m}$ ,  $H = 0.5 \text{ m}$ ,  $\beta=20^\circ$  and cohesions of: A) 0 kPa, B) 0.1 kPa, C) 1 kPa, and D) 10 kPa. Displacements are exaggerated for visualisation and should be interpreted as relative rather than absolute.

81x54mm (300 x 300 DPI)

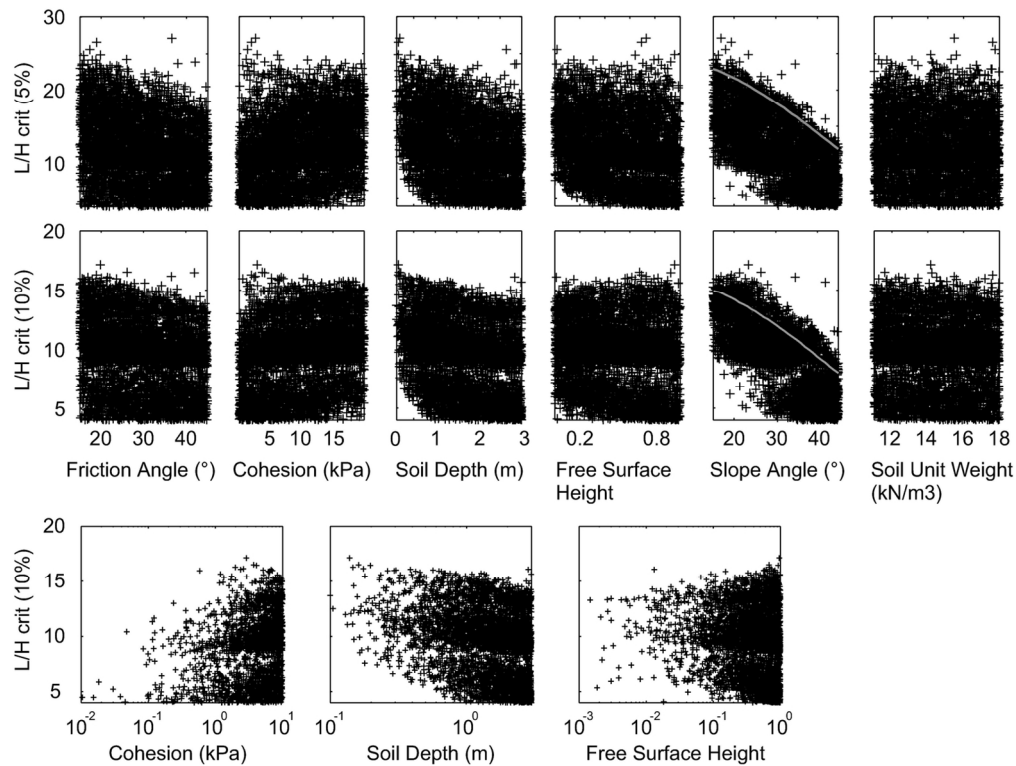


Figure 6: uncertainty plots showing variation in the length / depth ratio at which the infinite slope predictions converge to within 5 and 10% of the finite element predictions ( $L/H_{crit}$ ) for a range of: friction angles, soil cohesions, soil depths, normalised free surface heights, soil unit weights and slope angles. The bottom row shows results for parameters sampled to zero in semi-logarithmic space to illustrate their influence at low values. The grey lines on the slope angle plots have the equation  $y = a \cos^2(\beta)$ , where  $a = 24$  and  $16$  for the upper and lower plots respectively.

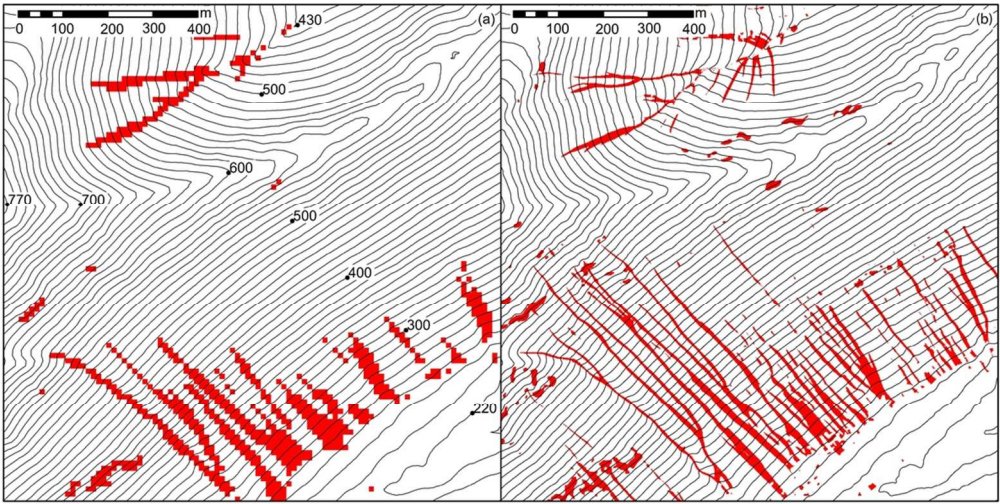


Figure 7: predicted landslides from a 1 km<sup>2</sup> patch of a grid based stability model with  $\phi'=40^\circ$ ,  $c'=1$  kPa,  $\gamma_{sat}=1.7$  kN m<sup>-3</sup>, transmissivity = 0.01 mm h<sup>-1</sup> and steady state rainfall rate = 100 mm h<sup>-1</sup>,  $H = 1$  m, cellsize is 10 m for a and 1 m for b.  
100x50mm (300 x 300 DPI)